

# COMBINED TRELLIS DECODER AND DECISION FEEDBACK EQUALIZER

## BACKGROUND

Equalizers are an important element in many diverse digital information applications, such as voice, data, and video communications. These applications employ a variety of transmission media. Although the various media have differing transmission characteristics, none of them is perfect. That is, every medium induces variation into the transmitted signal, such as frequency-dependent phase and amplitude distortion, multipath reception, other kinds of ghosting, such as voice echoes, and Rayleigh fading. In addition to channel distortion, virtually every sort of transmission also suffers from noise, such as additive white gaussian noise ("AWGN"). Equalizers are therefore used as acoustic echo cancelers (for example in full-duplex speakerphones), video deghosters (for example in digital television or digital cable transmissions), signal conditioners for wireless modems and telephony, and other such applications.

One important source of error is intersymbol interference ("ISI"). ISI occurs when pulsed information, such as an amplitude modulated digital transmission, is transmitted over an analog channel, such as, for example, a phone line or an aerial broadcast. The original signal begins as a reasonable approximation of a discrete time sequence, but the received signal is a continuous time signal. The shape of the impulse train is smeared or spread by the transmission into a differentiable signal whose peaks relate to the amplitudes of the original pulses. This signal is read by digital hardware, which periodically samples the received signal.

Each pulse produces a signal that typically approximates a sinc wave. Those skilled in the art will appreciate that a sinc wave is characterized by a series of peaks

centered about a central peak, with the amplitude of the peaks monotonically decreasing as the distance from the central peak increases. Similarly, the sinc wave has a series of troughs having a monotonically decreasing amplitude with increasing distance from the central peak. Typically, the period of these peaks is on the order of the sampling rate of the receiving hardware. Therefore, the amplitude at one sampling point in the signal is affected not only by the amplitude of a pulse corresponding to that point in the transmitted signal, but by contributions from pulses corresponding to other bits in the transmission stream. In other words, the portion of a signal created to correspond to one symbol in the transmission stream tends to make unwanted contributions to the portion of the received signal corresponding to other symbols in the transmission stream.

This effect can theoretically be eliminated by proper shaping of the pulses, for example by generating pulses that have zero values at regular intervals corresponding to the sampling rate. However, this pulse shaping will be defeated by the channel distortion, which will smear or spread the pulses during transmission. Consequently, another means of error control is necessary. Most digital applications therefore employ equalization in order to filter out ISI and channel distortion.

Generally, two types of equalization are employed to achieve this goal: automatic synthesis and adaptation. In automatic synthesis methods, the equalizer typically compares a received time-domain reference signal to a stored copy of the undistorted training signal. By comparing the two, a time-domain error signal is determined that may be used to calculate the coefficient of an inverse function (filter). The formulation of this inverse function may be accomplished strictly in the time domain, as is done in Zero Forcing Equalization ("ZFE") and Least Mean Square ("LMS") systems. Other methods

involve conversion of the received training signal to a spectral representation. A spectral inverse response can then be calculated to compensate for the channel distortion. This inverse spectrum is then converted back to a time-domain representation so that filter tap weights can be extracted.

In adaptive equalization the equalizer attempts to minimize an error signal based on the difference between the output of the equalizer and the estimate of the transmitted signal, which is generated by a “decision device.” In other words, the equalizer filter outputs a sample, and the decision device determines what value was most likely transmitted. The adaptation logic attempts to keep the difference between the two small. The main idea is that the receiver takes advantage of the knowledge of the discrete levels possible in the transmitted pulses. When the decision device quantizes the equalizer output, it is essentially discarding received noise. A crucial distinction between adaptive and automatic synthesis equalization is that adaptive equalization does not require a training signal.

Error control coding generally falls into one of two major categories: convolutional coding and block coding (such as Reed-Solomon and Golay coding). At least one purpose of equalization is to permit the generation of a mathematical “filter” that is the inverse function of the channel distortion, so that the received signal can be converted back to something more closely approximating the transmitted signal. By encoding the data into additional symbols, additional information can be included in the transmitted signal that the decoder can use to improve the accuracy of the interpretation of the received signal. Of course, this additional accuracy is achieved either at the cost of

the additional bandwidth necessary to transmit the additional characters, or of the additional energy necessary to transmit at a higher frequency.

A convolutional encoder comprises a  $K$ -stage shift register into which data is clocked. The value  $K$  is called the “constraint length” of the code. The shift register is tapped at various points according to the code polynomials chosen. Several tap sets are chosen according to the code rate. The code rate is expressed as a fraction. For example, a  $\frac{1}{2}$  rate convolutional encoder produces an output having exactly twice as many symbols as the input. Typically, the set of tapped data is summed modulo-2 (i.e., the XOR operation is applied) to create one of the encoded output symbols. For example, a simple  $K=3$ ,  $\frac{1}{2}$  rate convolutional encoder might form one bit of the output by modulo-2-summing the first and third bits in the 3-stage shift register, and form another bit by modulo-2-summing all three bits.

A convolutional decoder typically works by generating hypotheses about the originally transmitted data, running those hypotheses through a copy of the appropriate convolutional encoder, and comparing the encoded results with the encoded signal (including noise) that was received. The decoder generates a “metric” for each hypothesis it considers. The “metric” is a numerical value corresponding to the degree of confidence the decoder has in the corresponding hypothesis. A decoder can be either serial or parallel—that is, it can pursue either one hypothesis at a time, or several.

One important advantage of convolutional encoding over block encoding is that convolutional decoders can easily use “soft decision” information. “Soft decision” information essentially means producing output that retains information about the metrics, rather than simply selecting one hypothesis as the “correct” answer. For an

overly-simplistic example, if a single symbol is determined by the decoder to have an 80% likelihood of having been a “1” in the transmission signal, and only a 20% chance of having been a “0”, a “hard decision” would simply return a value of 1 for that symbol. However, a “soft decision” would return a value of .8, or perhaps some other value corresponding to that distribution of probabilities, in order to permit other hardware downstream to make further decisions based on that degree of confidence.

Block coding, on the other hand, has a greater ability to handle larger data blocks, and a greater ability to handle burst errors.

Figure 1 illustrates a block diagram of a typical digital communication receiver, including channel coding and equalization, indicated generally at 100. The receiver 100 comprises a demodulation and sync component 110, which converts the received analog signal back into a digital format. The receiver 100 further comprises an equalizer 120, an inner decoder 130, a de-interleaver 140, and an outer decoder 150. The inner coding is typically convolutional coding, while the outer coding is typically block coding, most often Reed-Solomon coding. The convolutional and block coding are generally combined in order to exploit the complementary advantages of each.

Figure 2 is a diagram of an equalizer 120 such as is commonly used in the digital receiver 100 shown in Figure 1. Typically, the equalizer 120 includes a controller 228, a finite impulse response (“FIR”) filter 222, a decision device 226, and a decision feedback equalizer (“DFE”) 224. The FIR filter 222 receives the input signal 221. The FIR filter 222 is used to cancel pre-ghosts—that is, ghost signals that arrive before the main transmission signal. The decision device 226 examines its inputs and makes a decision as to which one of the received signals at its input is the signal to be transmitted to the

output 229. The input to the decision device 226 is modified by a decision feedback equalizer 224, which is used to cancel post-ghosts—that is, ghost signals that arrive after the main transmission signal—and the residual signal generated from the FIR filter 222.

The decision device 226 is typically a hard decision device, such as a slicer. For example, in an 8VSB system, the slicer can be a decision device based upon the received signal magnitude, with decision values of 0,  $\pm 2$ ,  $\pm 4$ , and  $\pm 6$ , in order to sort the input into symbols corresponding to the normalized signal values of  $\pm 1$ ,  $\pm 3$ ,  $\pm 5$ , and  $\pm 7$ . For another example, the slicer can be multi-dimensional, such as those used in quadrature amplitude modulation (“QAM”) systems.

The controller 228 receives the input data and the output data and generates filter coefficients for both the FIR filter 222 and the decision feedback filter 224. Those skilled in the art will appreciate that there are numerous methods suitable for generating these coefficients, including LMS and RLS algorithms.

Figure 3 illustrates further details of one embodiment of the equalizer 120 shown in Figure 2. The input to the decision feedback equalizer 224 is output from the decision device 226, such as a slicer. The input data is delayed (F+M) stages, where F equals the number of stages in the FIR filter 222 and M equals the number of stages in the decision feedback equalizer 224. At each delay, the data is multiplied by the tap coefficients generated by the controller 228, and each of the results is summed with the output of the FIR filter 222. The equalizer 120 then passes the equalized data to a trellis decoder 350. An error signal 310 is generated by subtracting the input to the slicer 226 from its output. The error signal 310 is multiplied by a step size 320 before it is used to update the tap coefficients. Typically, the step size 320 is less than one, in order to permit the error

signal to iteratively adjust the coefficient taps over multiple cycles, so that variations in channel response and noise are averaged out. Generally, the smaller the step size, the more severe the transient conditions under which the equalizer 120 can converge, though at the cost of slower convergence.

Figure 4 shows the further details of one embodiment of a trellis encoder, shown generally at 400, suitable for use with the decision feedback equalizer 224 shown in Figure 3. The trellis encoder 400 is the 8VSB trellis encoder, precoder, and symbol mapper. As will be known by those skilled in the art, the 8VSB trellis encoder 400 uses an 8-level, 3-bit, one dimensional constellation. As can be seen from Figure 4, the 8VSB trellis encoder 400 uses a 2/3 rate trellis code.

Typically, the trellis decoder 350 uses a Viterbi algorithm to decode the signal encoded by the 8VSB trellis encoder 400. Typically, the trellis decoder 350 has a large number of stages—most often 16 or 24. The decoded output 229 is deinterleaved by the de-interleaver 140, and then sent to the outer decoder 150.

Figure 5 shows a typical trellis diagram for an 8VSB trellis code with n stages, shown generally at 500. The heavier line illustrates a current survive path. At each decoding clock cycle a new symbol is sent to the trellis decoder and the survive path is renewed. It will be appreciated that in a VSB system each sample contains one symbol, while in QAM or offset-QAM systems, each sample contains two symbols—one in the I channel, the other in the Q channel. However, regardless of the sample size, the coding and decoding is always performed symbol by symbol. At each stage a decision is made about which state is the most likely (i.e., which symbol was most likely transmitted), based on the survive path. For example, stage 1 gives the first estimation to the input,

and stage 2 gives the second estimation to the input, etc. It will be appreciated that the survive path may change based on the decoding process as each new input symbol is received, so that the survive path may not be the same (though shifted one symbol) from one input sample time to another.

Figure 6 shows the decoding error rate using a typical trellis decoder with the Viterbi decoding algorithm. As can be seen from the graph, when the system is running below the threshold, and even slightly above it, the error rate is lower after decoding, and the greater the decoding stage, the lower the error rate. The graph also shows that the early decoding stages have a higher gain than the later ones.

Figure 7 shows additional details of the equalizer 120. The error signal 310 is taken simply by subtracting a slicer output from a slicer input, then multiplying by the step size 320. The stepped error signal is then multiplied by the input to the FIR filter 222 and DFE 224, and the results sent to accumulators 710 to update the equalizer taps. This error signal only captures the variation between the input signal and the sliced data level. Whenever the sliced data level does not correspond to the originally transmitted data level, the error signal will incorrectly exclude the difference. For example, if a transmitted value of 3 is received as 4.2, the slicer will read the 4.2 as 5, with an error of  $-0.8$ . The correct error in this case is actually  $+1.2$ . The FIR filter 222 and DFE 224, which use the error signal to correct for channel distortion such as multipathing, will propagate that error.

As can be seen in Figure 3, in the prior art the DFE 224 is running independently from the trellis decoder 350. That is, the slicer 226 is in front of the trellis decoder 350 (with the DFE 224 between them). This arrangement has numerous disadvantages. In



particular, the decision feedback equalizer 224 works with the un-decoded signal, which has a higher error rate. The higher error rate in the input signal to the slicer 226 makes it slower to converge, and may actually cause divergence if the error rate is sufficiently high. Furthermore, it will cause the slicer to make incorrect decisions about the transmitted symbols, which it will pass on to the trellis decoder 350, where that error will be propagated. The gain of the equalizer will thereby be harmed even further.

What is needed is an equalizer in which the gain of the trellis decoder 350 is superior to what is produced when the data is sliced before decoding. In addition, an equalizer is needed in which the DFE does not rely on undecoded data. The present invention is directed towards meeting these needs, as well as providing other advantages over prior equalizers.

## SUMMARY OF THE INVENTION

A first embodiment adaptive equalizer comprises: a trellis decoder; a mapper coupled to the output of the trellis decoder; and a decision feedback equalizer coupled to the output of the mapper, the decision feedback equalizer having fewer than 16 taps. Each of the taps receives as input via the mapper output from a different one of the 16 stages of the trellis decoder.

A second embodiment adaptive equalizer comprises: a Viterbi decoder having 16 stages; a mapper coupled to the output of the Viterbi decoder; and a decision feedback equalizer coupled to the output of the mapper, the decision feedback equalizer having more than 16 taps. 16 of the taps each receive as input via the mapper output from a different one of the 16 stages of the Viterbi decoder.

A third embodiment adaptive equalizer comprises: a Viterbi decoder having 16 stages; a mapper coupled to the output of the Viterbi decoder; and a decision feedback equalizer coupled to the output of the mapper, the decision feedback equalizer having fewer than 16 taps. Each of the taps receives as input via the mapper output from a different one of the 16 stages of the Viterbi decoder.

A fourth embodiment adaptive equalizer comprises a decision feedback equalizer and a trellis decoder, wherein the decision feedback equalizer receives as input information from the trellis decoder.

A fifth embodiment adaptive equalizer consists of: an FIR filter; a trellis decoder coupled to the FIR filter; and a decision feedback equalizer coupled to the FIR filter and to the trellis encoder via a mapper. An output of the trellis decoder is mapped and scaled by the mapper and used by the equalizer to generate an error signal.

## BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a block diagram of a prior art digital receiver.

Figure 2 is a diagram of a prior art equalizer suitable for use in the digital receiver of Figure 1.

Figure 3 is a diagram showing further details of the prior art decision feedback equalizer in Figure 2.

Figure 4 is a diagram of a prior art 8VSB trellis encoder, precoder, and symbol mapper.

Figure 5 is a prior art trellis diagram.

Figure 6 is a graph showing the relationship between error rate and signal-to-noise ratio.

Figure 7 is a diagram of the prior art decision feedback equalizer of Figure 3, showing a trellis diagram having  $n$  stages.

Figure 8 is a diagram of a decision feedback equalizer according to the present invention.

Figure 9 is a diagram of a preferred embodiment trellis code interleaver according to the present invention.

Figure 10 is a diagram of a preferred embodiment trellis code de-interleaver according to the present invention.

Figure 11 is a diagram of the structure of a preferred embodiment combined decision feedback equalizer and trellis decoder according to the present invention with 12 parallel trellis decoders and 16 decoding stages.

Figure 12 is a diagram of the output of the decision feedback equalizer of Figure 11.

Figure 13 is a diagram showing additional details of the decision feedback equalizer of Figure 11.

Figure 14 is a diagram of certain elements of a preferred embodiment equalizer according to the present invention.

Figure 15 is diagram of a preferred embodiment equalizer according to the present invention having 12 parallel trellis decoders and 16 decoding stages.

## DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

For the purposes of promoting an understanding of the principles of the invention, reference will now be made to the embodiment illustrated in the drawings and specific language will be used to describe the same. It will nevertheless be understood that no limitation of the scope of the invention is thereby intended, and alterations and modifications in the illustrated device, and further applications of the principles of the invention as illustrated therein are herein contemplated as would normally occur to one skilled in the art to which the invention relates. In particular, although the invention is discussed in terms of an 8VSB system, it is contemplated that the invention can be used with other types of modulation coding, including, for example, QAM and offset-QAM.

Figure 8 illustrates a first embodiment equalizer according to the present invention, indicated generally at 800, employing a decoding structure in which the decision feedback equalizer 850 receives its input from the trellis decoder 350. In certain embodiments, the trellis decoder 350 uses a Viterbi algorithm, as is known in the art. The trellis decoder output 803 is input to the decision feedback equalizer 850 via a mapper 810. The mapper 810 maps and scales the trellis decoder's 350 output 803 back to signal levels. For example, in 8VSB the mapper 810 maps and scales the trellis decoder's 350 output 803 back to normalized signal levels of  $\pm 1$ ,  $\pm 3$ ,  $\pm 5$ , and  $\pm 7$ . In certain embodiments the trellis decoder 350 has 16 stages and the decision feedback equalizer 850 has M taps. In these embodiments, from the 17th tap up to the Mth tap the decision feedback equalizer 850 has the same structure as a traditional decision feedback equalizer 224, except that the input to this section is the mapped and scaled output from

the 16th stage of the trellis decoder. From the 1st tap to the 16th tap the inputs to the DFE 850 are the mapped and scaled output 803 from the 1st to 16th stages of the trellis decoder 350, respectively. As can be seen from Figure 8, for each input symbol there is a survive path (highlighted as a heavier line in Figure 8). The inputs to the DFE 850 from stage 1 to stage 16 are the mapped and scaled decoded output on the survive path.

In certain other embodiments the trellis decoder 350 has some other number of stages “n,” and the DFE 850 has M taps. In these embodiments, the decision feedback equalizer 850 has the same structure from the (n+1)th tap up to the Mth tap, and from the 1st tap to the nth tap the inputs to the DFE 850 are the mapped and scaled output from the trellis decoder 350 from the 1st to the nth stage, respectively.

It will be appreciated that the current survive path can change based on the decoding process with each new input symbol, so the survive path may not be the same (though shifted one symbol) from one sample time to the next. Thus, all the inputs to the DFE 850 can vary from symbol to symbol. This is different from prior art DFEs 224, in which the input to the next stage in the DFE 224 is the delayed symbol from the previous stage.

In certain of these embodiments the equalizer taps are generated as shown in Figure 7. The error signal 310 is taken by subtracting a slicer input from a slicer output. The error signal is then multiplied by the step size 320. The results are multiplied by the input to the FIR filter 222 and DFE 224 and sent to accumulators 710 to update the equalizer taps.

Preferably, the equalizer taps are generated differently, as shown in Figure 8. The raw error signal is taken by subtracting a delayed version of the input to the trellis

decoder 350 from the mapped and scaled output 229 of the trellis decoder 350 by an error summer 860. The raw error signal is then multiplied by the step size 320. The result is then multiplied by the same input to the trellis decoder that was supplied to the summer 860 (to be subtracted from the mapped and scaled output 229) to generate the corrected error signal. Note that this input to the trellis decoder must be delayed again by the same number of cycles it takes for the error signal 860 to be multiplied by the step size 320. The result is then sent to the accumulators 820 to update the equalizer taps.

In certain other embodiments, the error signal is taken by subtracting a delayed version of the input to the trellis decoder 350 from a mapped and scaled output 803 of one of the stages of the trellis decoder 350.

Those skilled in the art will appreciate that some encoding schemes have multiple independent encoders running in parallel, including the 8VSB system (which employs 12 such parallel encoders). Typically, trellis code intrasegment interleaving is used in such systems. This uses a corresponding number of identical trellis encoders and precoders operating on interleaved data symbols. In a system with 12 parallel encoders, for example, the code interleaving is accomplished by encoding the 0th, 12th, 24th...symbols as one group, the 1st, 13th, 25th...symbols as a second group, the 2nd, 14th, 26th...symbols as a third group, and so on for a total of 12 groups.

Figure 9 illustrates a trellis code and precoder intrasegment interleaver, shown generally at 900, that feeds a mapper such as the one shown in Figure 4. Bytes are fed from the byte interleaver (or multiplexer) 910 to the trellis encoder and precoders 920, and they are processed as whole bytes by each of the twelve encoders 920. Each byte produces four symbols from a single encoder 920. These bytes are all assembled into a

single bit stream a demultiplexer 930. The 8VSB receiver uses 12 trellis decoders in parallel, each receiving every 12th symbol, as shown in Figure 10. The bit stream is again interleaved by a multiplexer 1010, fed to the parallel decoders 1020, and then reassembled into a single bit stream by a demultiplexer 1030.

Figure 11 illustrates the preferred embodiment structure of the combined DFE 850 and trellis decoder 350 with 12 independent parallel trellis decoders, each having 16 decoding stages, indicated generally as 1100. (It will be appreciated that a different number of trellis decoders, or trellis decoders having a different number of stages, or both, can also be used.) There is one input multiplexer and there are 16 output demultiplexers. The position of the multiplexer and the de-multiplexers move from 0 to 11 and back to 0 in synchronization. Thus, when the input multiplexer is connected to decoder 0 all the output de-multiplexers are connected to decoder 0, and so on. The output to the decision feedback equalizer 224, indicated as stage 1, stage 2, and up to stage 16 are taken from the de-multiplexer output. Thus, when all the de-multiplexers are connected to decoder 3, for example, the output to the decision feedback equalizer 224 is taken from the third trellis decoder, decoding stages 1 to 16. As shown in the figure, each independent decoder runs independently. For example, the symbols fed to decoder 3 (1/12 the total symbol rate, of course) stay in decoder 3 all the time, while each de-multiplexer takes the output from one of the 12 decoders.

Figure 12 illustrates the decoding outputs placement in a DFE 850 with 12 parallel trellis decoders and 16 decoding stages, indicated generally at 1200. Thus, the DFE 850 has at least 192 taps, and a total of at least 192 symbols' delay. During the first 192 delay elements there are a total of 16 banks 1210. Each bank has 12 symbol delay



elements, or 12 taps. The input to the first element in the first bank (delay element 0) is taken from the mapped and scaled output of stage 1 of the trellis decoder. The input to the first element in the second bank (delay element 12) is taken from the mapped and scaled output of stage 2 of the trellis decoder, and so on, until the input to the first element in the 16th bank (delay element 180) is taken from the mapped and scaled output of stage 16 of the trellis decoder. In each of the 16 banks, therefore, there are 12 delay elements.

Figure 13 is a diagram of the banks of the combined decision feedback equalizer shown in Figure 11. It will be appreciated that each of the 16 banks has the structure of prior 12-tap decision feedback equalizers. Thus, the input to the 2d and up to the 12th tap are a version of a previous symbol, but delayed by one symbol, as shown in Figure 8. However, the input into the 1st tap is taken from the output of the trellis decoder.

Those skilled in the art will appreciate that any number of parallel encoders and decoders may be used in a decision feedback equalizer according to the present invention. For example, a decision feedback equalizer having 16 parallel encoders and decoders, the trellis code interleaver and de-interleaver will have essentially the same structure as shown in Figures 9 and 10, except, of course, that there will be a total of 16 trellis encoders and pre-coders between the byte interleaver and the mapper, and 16 trellis decoders between the decoder input multiplexer and the de-multiplexer. Of course, the multiplexers and de-multiplexers will all be 16-to-1, instead of 12-to-1. Likewise, the structure will differ from what is shown in Figure 11 only in that there will be 16 parallel decoders (and 16-to-1 multiplexers and de-multiplexers). The decoding output will, of course, have a delay of 256 symbols, instead of the 192 shown in Figures 12 and 13. The

first bank will receive delay elements 0-15, the second bank will receive delay elements 16-31, and so on.

It will also be appreciated that a decision feedback equalizer according to the present invention can have fewer taps than the total trellis decoder decoding length. For example, if the decision feedback equalizer has 96 taps, while the trellis decoder has 12 parallel encoders and decoders and 16 decoding stages, the decision feedback equalizer can take the mapped and scaled output from the first 8 trellis decoder stages. There will be a total of 96 delay elements. The error signal is preferably generated from the mapped and scaled output of the last decoding stage.

It will be appreciated that the error signal in an equalizer according to the present invention is generated with a short delay. If the error signal is generated after 16 decoding stages in an 8VSB system, for example, the delay is 192 symbols, as shown in Figures 11 and 12. With a symbol rate of 10.76MHz the delay is about 17.8 $\mu$ s.

Compared with a maximum channel distortion varying rate of about 200Hz, or 5ms, the delay in generating the error signal is very short. Thus, the delay in error signal generation will not substantially harm convergence due to the varying channel distortion.

Furthermore, if the number of parallel encoders and decoders is sufficiently large so that the total delay is long enough to harm the tracking of varying channel distortion, the error signal can be generated at earlier decoding stages. The earlier stages have higher error rate than the last decoding stage, so this is preferable only when necessary to reduce the delay in error signal generation. However, even the earlier decoding stages have a significant gain. Therefore, the result will still be a substantially improved

decoding gain over a system in which, for example, the input to the trellis decoder is a sliced signal.

Figure 14 illustrates a preferred embodiment equalizer according to the present invention, indicated generally at 1400. It is similar to the equalizer shown in Figure 8, except that after the raw error signal is multiplied by the step size 320, the result is not multiplied by a delayed version of the input to the trellis decoder 350. Instead, it is multiplied by the mapped and scaled output 229 of the trellis decoder 350.

Figure 15 illustrates certain elements of an equalizer, shown generally as 1500, similar to the one shown in Figure 14, but having 12 parallel trellis decoders and 16 decoding stages. Thus, it is similar to the equalizer shown in Figure 13, except that the stepped error signal is multiplied by the mapped and decoded output of the trellis decoder 350, rather than its input.

Because the output 229 of the trellis decoder 350 more closely corresponds to the transmitted signal, the coefficient taps are more accurately updated. Thus, the decoding gain of the trellis decoder 350 is propagated through the error feedback, further improving the performance of the trellis decoder 350. Also, because the decoded output 229 of the trellis decoder has fewer bits than its input, simpler hardware may be used.

Those skilled in the art will appreciate that an equalizer according to the present invention has advantages over prior art equalizers. The input to the decision feedback equalizer has fewer errors, because it is taken from the mapped and scaled output of the trellis decoder. The lower error rate in the trellis decoder's input makes the equalizer more stable, and causes it to converge more rapidly. Also, the lower error rate in the trellis decoder's input results in a much lower error rate in its output, resulting in a better

equalized signal. Furthermore, the equalizer more effectively eliminates long post-ghosts because there is increasing gain from the trellis decoder from stage to stage. There is significant gain starting from the first trellis decoding stage, so that the decision feedback equalizer is benefited at start-up. Also, since the trellis decoded output is more reliable and accurate, the input to the decision feedback equalizer can have fewer bits. This permits a reduction in hardware complexity.

It will further be appreciated that these advantages can be achieved without the use of additional hardware, except for a delay line for generating error signals from the decoder output. A standard trellis decoder employing a standard Viterbi algorithm can be used.

While the invention has been illustrated and described in detail in the drawings and foregoing description, the same is to be considered as illustrative and not restrictive in character, it being understood that only the preferred embodiment has been shown and described and that all changes and modifications that come within the spirit of the invention are desired to be protected.